

*Misprints and corrections*

p.6 The last 2.5 lines in the proof of Theorem 1.2.1 should be:  
Change  $\lceil \frac{d}{2} \rceil$  of the nonzero positions to zeroes to obtain  $y$ . Then  $d(0, y) \leq d - \lceil \frac{d}{2} \rceil \leq t$  and  $d(c, y) = \lceil \frac{d}{2} \rceil \leq \lceil \frac{2t}{2} \rceil = t$ , but  $0 + y = c + (y - c)$  so the code is not  $t$ -error correcting.

p.6 just after Lemma 1.2.3 : Lemma 1.2.3 should be Lemma 1.2.2

p. 14 Problem 1.5.8 : Example 1.1.2 should be Example 1.1.4

p. 26 line -6  $(a_0, a_1, \dots, a_m)$  should be  $(a_0, a_1, \dots, a_m) \neq (0, 0, \dots, 0)$

p.27-28 Theorem 2.3.6 and proof  $i \in c_j$  should be  $i \in C_j$  and  $f_j(x)\mathbb{F}_2[x]$  should be  $f_j(x) \in \mathbb{F}_2[x]$ ,  $(\beta^j)^i$  should be  $\beta^i$ .

p. 28 Algorithm 2.3.1 step 4  $i \in c_j$  should be  $i \in C_j$

p. 36 Figure 3.1 Caption 1.8  $s = 1$  should be  $l = 1$

p. 46 1.12  $\frac{w}{N}$  should be  $\frac{w}{n}$ .

p. 50 1.12 Theorem 2.2.1 should be Theorem 2.2.2.

p. 52 1.13  $\sum_{j=1}^{l_1} Q_{1,j}$  should be  $\sum_{j=0}^{l_1} Q_{1,j}$

P. 53 Example 5.2.1 The received vector should be  $r = (5, 9, 0, 9, 0, 1, 0, 7, 0, 5)$  and 11 unknowns should be 12 unknowns.

p.55 the polynomial  $P^{(S)}(x)$  should have been:

$$P^{(S)}(x) = \sum_{r=1}^t p_r^{(S)} x^r = (-1)^{t-S} x \prod_{m=1, m \neq s}^t (x - x_{i_m}) \quad (1)$$

The last part of the proof should be:

$= x_{i_1} \cdots x_{i_{s-1}} \cdot x_{i_{s+1}} \cdots x_{i_t} \prod_{1 \leq l < s < j \leq t} (x_{i_j} - x_{i_l}) (-1)^{t-S} x \prod_{m=1, m \neq s}^t (x - x_{i_m})$   
by Corollary 5.3.1 and hence

$d = x_{i_1} \cdots x_{i_{s-1}} \cdot x_{i_{s+1}} \cdots x_{i_t} \prod_{1 \leq l < s < j \leq t} (x_{i_j} - x_{i_l}) P^{(s)}(x)$   
so by replacing the  $x^j$  with  $S_j$  the claim follows.  $\square$

p.57 l.16 Section 5.2 should be Section 5.3

p.57-60. Here we suppose that  $d$  is odd. If  $d$  is even  $l_1$  should be replaced with  $l_1 - 1$ .

p.61 (Example 5.2.1) should be (Example 5.2.1 continued)

p.61 Example 5.4.1 the error polynomial should be  $x^9 + 3x^3$  and  $c(x) = r(x) - e(x)$

p.67 Example 6.3.1 last line, last sentence should be “and this is the true minimum distance, since  $g(x) = x^9 + x^6 + 1$ ”.

p.79 l.6:  $\frac{37}{64} = 0.58$  should be  $\frac{36}{64} = 0.56$

p.85 after Definition 8.1.5  $(M + 1)n$  should be  $(M + 1)\frac{n}{k}$  and  $kM$  should be  $M$

p.87 line 19 after “reversing  $g$ ” add “Note that the reversal should include all blocks affected so for an odd  $m + 1$ , the length of the  $g$  sequence is extended by 1.”

p.88 Example 8.3.2 line 7 length 5 should be length 6

p.88 Definition 8.3.2 last line should be “where  $s_j$  is calculated only for the  $n - k$  parity positions in each  $n$ -block, and where  $s_j = 0$  if  $r$  is a code-word.”

p.89 line 21  $j = \lfloor R(N' - m) \rfloor$  should be  $j = \lfloor R(N' - m - 1) \rfloor + k$

p.89 Lemma 8.4.1 “decreasing” should be “non-increasing”

p.90 lines 9 and 10 Lemma 8.4.1 should be Lemma 8.4.2

p.90 Theorem 8.4.2  $j = \lfloor R(N' - m) \rfloor$  should be  $j = \lfloor R(N' - m - 1) \rfloor + k$

p.90 Example 8.4.1 replace “(11,1), (14,2), (17,3)” with “(12,1), (15,2), (18,3)” and the upper bound is now 10 instead of 9

p.91 replace  $\sum_{i \geq 0} G_i u_{j-i}$  with  $\sum_{i \geq 0} u_{j-i} G_i$

p.93 after (8.5) “ $k - m$  by  $m$  matrix” should be “ $k - m$  by  $n$  matrix”.

p.96 Problem 8.8.8 1) should be: Show that  $g_0$  is irreducible, while  $g_1$  factors into two irreducible polynomials.

p.96 Problem 8.8.9 1) "binary" should be "irreducible".

p.97 Chapter 9. The methods and definitions in this chapter are only for codes with rate  $R = 1/n$ . Similar concepts may be used for codes with  $R = k/n$ , but we prefer to create such codes by puncturing as shown in Section 8.5.

p.98 Example 9.1.2 The matrix should be:

$$\Phi = \begin{bmatrix} 00 & - & 11 & - \\ 11 & - & 00 & - \\ - & 10 & - & 01 \\ - & 01 & - & 10 \end{bmatrix} \quad (2)$$

p.99 Lemma 9.1.3 "length  $N$ " should be "length  $K$ ".

p. 101 Example 9.1.4 The system of equations should be:

$$\begin{bmatrix} 0 & 0 & z^2 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & z & 0 & z \\ 0 & z & 0 & z \end{bmatrix} \begin{bmatrix} \rho_0 \\ \rho_1 \\ \rho_2 \\ \rho_3 \end{bmatrix} = \begin{bmatrix} \rho_0 \\ \rho_1 - z^2 \\ \rho_2 \\ \rho_3 \end{bmatrix} \quad (3)$$

p.102 lines 8 and 11  $r$  should be  $r_j$ .

p.102 line 11 add "Symbols punctured away should not be considered in the calculation. In this way the following Algorithm 9.2.1 may also be applied to punctured codes with rates  $R = k/n$  for  $k \neq 1$ "

p 103 line 4  $P[r]$  should be  $P[r_j]$

p 103 4 to 5 lines before (9.5) " $2^k$ " should be "two"

p.103 (9.5)  $\mu_{i'}(j-1)$  should be  $\mu_i(j-1)$

p.105 Figure 9.1.  $\mu_1(j)$  under  $j = 3$  should be 5.  $\mu_2(j)$  and  $\mu_3(j)$  under  $j = 4$  should be 7 and 6. The last two lines under 5 6 7 should be 6 4 8 and 7 7 7.

p.105 Figure 9.1 Caption "between time 4 and 5" should be "between time 3 and 4"

p.107 Problem 9.3.3 4)  $A = BC^*$  should be  $A = BC\star$

p.110 lines 9-10 "A minimum distance codeword of weight  $d_1 \dots$ " should be "A codeword of minimum weight  $d_1 \dots$ "

p.113  $P(t) = e^\mu \dots$  should be  $P(t) = e^{-\mu}$

p.120 Lemma 11.1.1 "For all  $i \geq -1$ " should be For all  $i \geq 0$ .

p.121 1.16  $S(X)$  should be  $S(x)$

p. 122 lines 2-17 should be replaced by: The syndromes are  $S_1 = r(\alpha) = 1 + \alpha + \alpha^2 + \alpha^4 = \alpha^2$   
 $S_2 = S_1^2 = \alpha^4$   
 $S_3 = r(\alpha^3) = 1 + \alpha^3 + \alpha^6 + \alpha^{12} = \alpha^9$   
 $S_4 = S_2^2 = \alpha^8$   
 $S_5 = r(\alpha^5) = 1 + \alpha^5 + \alpha^{10} + 1 = \alpha^5$   
 $S_6 = S_3^2 = \alpha^3$

We therefore have  $S(x) = \alpha^2 x^5 + \alpha^4 x^4 + \alpha^9 x^3 + \alpha^8 x^2 + \alpha^5 x + \alpha^3$ .

The Euclidian algorithm on  $x^6$  and  $S(x)$  gives:

$i$	$g_i$	$r_i$	$q_i$
-1	0	$x^6$	-
0	1	$\alpha^2 x^5 + \alpha^4 x^4 + \alpha^9 x^3 + \alpha^8 x^2 + \alpha^5 x + \alpha^3$	-
1	$\alpha^{13} x + 1$	$\alpha^3 x^4 + \alpha^5 x^3 + \alpha^{13} x^2 + \alpha^2 x + \alpha^3$	$\alpha^{13} x + 1$
2	$\alpha^{12} x^2 + \alpha^{14} x + 1$	$\alpha^8 x^3 + \alpha^{10} x^2 + \alpha x + \alpha^3$	$\alpha^{14} x$
3	$\alpha^7 x^3 + \alpha^9 x^2 + \alpha^9 x + 1$	$\alpha^7 x^2 + \alpha^{14} x + \alpha^3$	$\alpha^{10} x$

From this we see that  $j = 3$  and  $g_3(x) = \alpha^7 x^3 + \alpha^9 x^2 + \alpha^9 x + 1$ , which has  $\alpha^5, \alpha^8$  and  $\alpha^{10}$  as zeroes, so the error vector is  $x^{10} + x^8 + x^5$  and the codeword is therefore  $1 + x + x^2 + x^4 + x^5 + x^8 + x^{10}$  ( $= g(x)$ ).

p.122 Example 11.2.2  $S_4$  should be  $S_4 = \dots = \alpha^6$

p.123 the last line should be:

$$P^{(S)}(x) = \sum_{r=1}^t P_r^{(S)} x^r = (-1)^{t-S} x \prod_{l=1, l \neq S}^t (x - x_{i_l}) \quad (4)$$

and

$$S_r = \sum_{j=1}^t e_{i_j} x_r^{i_j}. \quad (5)$$

p.124 line 6 should be:

$$g'_j(x_{i_S}) = \prod_{l=1, l \neq S}^t (x - x_{i_l}) = x_{i_S}^{-1} (-1)^{(t-S)} P^{(S)}(x_{i_S}) \quad (6)$$

p. 124 lines 10-14 should be: and therefore

$$\begin{aligned} r_j(x) &= \prod_{l=1}^t (x - x_{i_l}) \sum_{i=1}^{2t} S_i x^{2t-i} \bmod x^{2t} \\ &= (-1)^{t-S} P^{(S)}(x) x^{-1} (x - x_{i_S}) \sum_{i=1}^{2t} S_i x^{2t-i} \bmod x^{2t} \\ &= (-1)^{t-S} (x - x_{i_S}) \sum_{i=1}^{2t} \sum_{r=1}^t P_r^{(S)} x^{r-1} S_i x^{2t-i} \bmod x^{2t} \end{aligned}$$

and hence

$$r_j(x_{i_S}) = -(-1)^{(t-S)} \sum_{r=1}^t x_{i_S}^{2t} P_r^{(S)} S_r \quad (7)$$

and the result follows.  $\square$

p.124 line 4 from below:  $e_1$  should be  $e_1 = (1)^{-7}.. = \alpha$ .

p.128 l.21 condition (12.2) should be condition 2

p.128 (12.3)  $\geq 0$  should be  $> 0$

p.128 (12.4)  $\leq$  should be  $<$ .

p.129 last line of Algorithm 12.1.1 should be  $d(f(x_1), f(x_2), \dots, f(x_n)), (r_1, r_2; \dots, r_n)) \leq \tau$

p.130 l.19 " $\leq$ " should be " $=$ "

p.130 l. -7  $w_i$  should be  $r_i$

p.131 (12.5)  $\geq$  should be  $>$

p.131 (12.6)  $\leq$  should be  $<$

p.131 (12.9)  $\leq$  should be  $<$ .

p.131 l.4  $l > a$  or  $b > l_a$  should be  $b > l$  or  $a > l_a$

p.131 line 8 from below Gurusami should be Guruswami.

p.131 l.-2  $Q_{j,r}$  should be  $Q_{r,j}$ .

p.132 l.2  $< \tau$  should be  $\leq \tau$

p.133 l.-13  $\alpha^{10}x^{10}$  should be  $\alpha^2x^{10}$

p.133 l.-2"  $\alpha^{11} + x^6$  should be  $\alpha^{11}x^6$

p.137 l.-1 " row indices" should be " row indices u"

p.138 l.1 "column indices such that  $h_{uv} = 1$  for  $v$  in  $J_u$ " should be " column indices  $v$  such that  $h_{uv} = 1$  for row  $u$ "

p. 140 l.20 the sentence i.e..... is superfluous and can be deleted.

p.141 l.6 symbol node  $\nu$  should be symbol node  $v$ .

p.142 l.7  $a_v(c_v) = r_v + 1$  should be  $a_v(x) = r_v + x$

p.148 Example 13.4.1  $a(j)$  should be  $a_j$ ,  $\mu_1$  and  $\mu_2$  should be  $m_1$  and  $m_2$ .

p.152 line 16 from above: the scnd type of points should be  $(\alpha^{i+j(q-1)}, \beta_i)$

p. 152 l.-3  $\rho : \mathbb{F}_{q^2}[x, y]$  should be  $\rho : \mathbb{F}_{q^2}[x, y] \rightarrow \mathbb{N}_0$

p.154 line 9 from below: The element in the last sum should be:  $(\alpha^{i+j(q-1)})^{a_1+a_2}$ .

p.154 line 5 from below: The element in the first sum should be  $\alpha^{j(a_1+a_2)}$ .

p.155 Example 14.1.1  $s = 10, 11, \dots, 50$  should be  $s = 11, 12, \dots, 51$ .

p.156 l.6 " and .....then have" should be deleted.

p.156 l.7, l.17 and l.18  $r(P_j)$  should be  $r_j$

p.157 Problem 14.3.5 Theorem 14.4.1 should be Lemma 14.4.1

p.160 (A.4) change signs in the two terms.

p.163 Problem 1.5.2 3) should be  $G(111111)^T = (110)^T \neq (000)$ .

p.165 Problem 1.5.9 1)  $g_{34}$  should be 1

p.165 Problem 1.5.10 1)  $d^* = d$  if all minimum weight words have a zero in the deleted position, else  $d^* = d - 1$

2)  $d^* \geq d$ .

p.165 Problem 1.5.11  $H_c$  should be  $H$

p.170 Problem 5.5.2 2) The last two columns of  $G$  should be:

6 2  
2 2  
2 5  
5 6

p.171 Problem 5.5.3 1) The second coordinate of the sum should be  $\alpha^4$ .

p.172 Problem 6.5.3)  $H$  should have been:

$$H = \begin{bmatrix} 1 & 0 & 0 & 1 & 1 & 0 & 1 & 0 & 1 & 1 & 1 & 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 1 & 1 & 0 & 1 & 0 & 1 & 1 & 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 1 & 1 & 0 & 1 & 0 & 1 & 1 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 1 & 1 & 0 & 1 & 0 & 1 & 1 & 1 & 1 \end{bmatrix}$$

p.173 Problem 8.8.1 1) should have been: 11.10.10.10.00.00.10.11

p.174 Problem 8.8.2 3) should have been: 001.010.011.001.101

p.174 Problem 8.8.4 should have been:

1)

$$H = \begin{bmatrix} 0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 1 \\ 1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 1 \\ 0 & 1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 1 & 1 & 1 & 1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

2) Yes

p.175 Problem 8.8.7 should have been: 1) For the code of Problem 8.8.1:

$$G = (1 + D + D^3, 1 + D^2 + D^3)$$

$$H = (1 + D^2 + D^3, 1 + D + D^3)$$

for the code of problem 8.8.2:

$$G = (1 + D + D^2, 1 + D^2, 1 + D)$$

$$H = \begin{bmatrix} 1 + D & 1 + D^2 \\ 0 & 1 + D \end{bmatrix}$$

- p.175 Problem 8.8.8 should have been: 1)  $g_1(D) = (1 + D)(1 + D + D^3)$   
 2) short information sequences give weight at least 3 from  $g_0$  and at least 4 from  $g_1$ .  
 3) The encoded sequence is 11.10.10.00.00.00.10.11.00 and has weight 7.  
 4) 3.

p.180 Problem 12.4.1 2) should be  $\tau \leq 10$  !

p.180 Problem 12.4.2  $k$  should be 5 and  $l = 3$  gives  $\tau \leq 17$ .

p.181 Problem 12.4.3 2) The first matrix should have 10 rows, the ninth should be :139541.

p.181 last line The second codeword is (0, 0, 6, 9, 1, 6, 1, 8, 2, 9)

p.182 Problem 13.5.1 The parity bits should be (0011001001)

p. 183 Problem 14.3.1 4) should be.  $H(27)^\perp = H(47)$

p.183 Problem 14.3.5 The last 4 lines should be: with  $h = 1$ . So ..  

$$\sum_{i=0}^{q-2} \alpha^{i(q+1)} \sum_{\beta^q + \beta = \alpha^{i(q+1)}} \beta^{b_1 + b_2}$$

$$= \sum_{i=0}^{q-2} \alpha^{i(q+1)} (\alpha^{i(q+1)})^{b_1 + b_2} \sum_{\beta^q + \beta = 1} \beta^{b_1 + b_2}$$

$$= \frac{\alpha^{(q+1)(1+b_1+b_2)(q-1)-1}}{\alpha^{(q+1)(1+b_1+b_2)-1}} \sum_{\beta^q + \beta = 1} \beta^{b_1 + b_2} = 0$$
 ,when the denominator is nonzero,

In the remaining case we get with  $1 \leq a \leq q - 1$   

$$- \sum_{\beta^q + \beta = 1} \beta^{a(q-1)-1} = - \sum_{\beta^q + \beta = 1} \beta^{(a-1)q + q - a - 1} = - \sum_{\beta^q + \beta = 1} (\beta^{q-a-1})(1 - \beta)^{a-1} = - \sum_{\beta^q + \beta = 1} (\beta^{q-a-1}) \sum_{j=0}^{a-1} \binom{a-1}{j} (-1)^{a-1-j} \beta^{q-2-j} = 0$$

since  $\sum_{\beta^q + \beta = 1} \beta^s = 0$  when  $s < q - 1$  as we will now prove:

$\sum_{\beta^q + \beta = 1} \beta^s = \sum_{\alpha^q + \alpha = 0} (\gamma + \alpha)^s$ , where  $\gamma$  is a fixed element with  $\gamma^q + \gamma =$

1. So we get:

$$\begin{aligned} & \sum_{\alpha^q + \alpha = 0} (\gamma + \alpha)^s \\ &= \sum_{\alpha^q + \alpha = 0} \sum_{j=0}^s \binom{s}{j} \gamma^{s-j} \alpha^j \\ &= \sum_{j=0}^s \binom{s}{j} \gamma^{s-j} \sum_{\alpha^q + \alpha = 0} \alpha^j \\ &= 0 \end{aligned}$$

p.185 line 6 from above: 1. should be : 1. Choose the field, by choosing  $m$ .



p.194 line 7 from below in the second column insert Viterbi algorithm  
104.